

## Notes Section 2.8 Solving Inequalities in One Variable - Polynomial Inequalities

Examples:

- 1) Determine the x-values that cause the polynomial function to be
  - zero
  - positive  $f(x) > 0$
  - negative  $f(x) < 0$

$$f(x) = (2x^2 + 5)(x - 8)^2(x + 1)^3$$

Using a SIGN CHART

Process

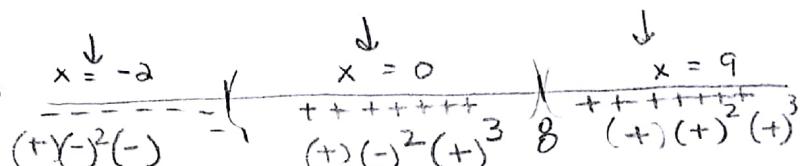
$$\begin{aligned} 2x^2 + 5 &= 0 \\ \sqrt{x^2} &= \sqrt{-\frac{5}{2}} \\ x &= \text{not real} \end{aligned}$$

$$x - 8 = 0$$

$$x + 1 = 0$$

$$x = -1$$

- 1) Find the key numbers and draw a number line arranging the key numbers from least to greatest
- 2) Determine the test intervals
- 3) Choose an x value in each interval to test
- 4) Interpret the results and answer all questions



a) zeros  $x = -1, x = 8$

b) pos  $f(x) > 0$   $(-1, 8) \cup (8, \infty)$

c) neg  $f(x) < 0$   $(-\infty, -1)$

- 2) Solve the polynomial inequality using a sign chart. Factor first!

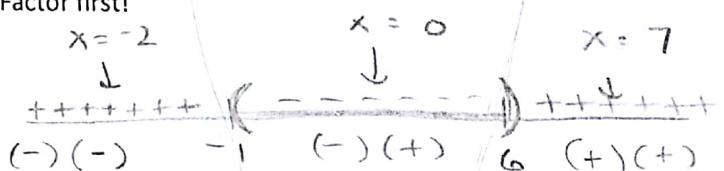
$$x^2 - 5x - 6 < 0$$

$$(x - 6)(x + 1) < 0$$

Zeros  $x = 6$   $x = -1$  test intervals:  $(-\infty, -1)$   $(-1, 6)$   $(6, \infty)$

$x^2 - 5x - 6 < 0$  for the interval

$$(-1, 6)$$

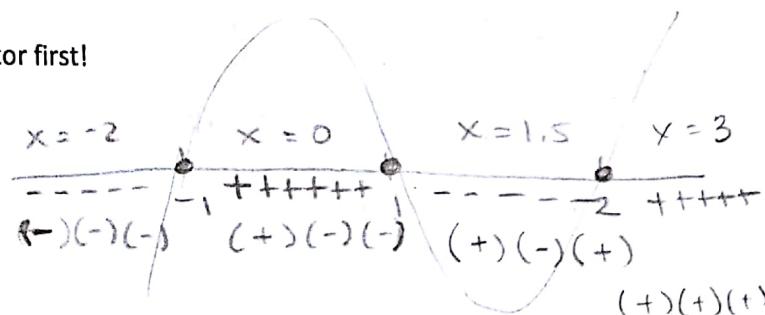


- 3) Solve the polynomial inequality using a sign chart. Factor first!

$$(x+1)(x^2 - 3x + 2) \geq 0$$

$$(x+1)(x-2)(x-1) \geq 0$$

Zeros:  $x = -1$   $x = 1$   $x = 2$



So  $(x+1)(x^2 - 3x + 2) \geq 0$  for intervals

$$[-1, 1] \cup [2, \infty)$$

What is the degree?  
Show me what behavior will arms